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**The research of the dynamic properties of rotating units  
in turbochargers****Key words**

Turbocharger, rotating unit, sliding bearing with a floating ring bearing, rigidity and damping factor.

**Słowa kluczowe**

Turbosprężarka, zespół wirujący, łożysko ślizgowe z panewką pływającą, współczynniki sztywności i tłumienia.

**Summary**

The dynamic model of a rotating unit of a turbocharger has been designed. Both masses of the rotors and shaft have been modelled as concentrated masses. The rotating unit has been propped on two supports forming lateral sliding bearings with a floating ring bearing. Each bearing is designed including the floating ring bearing mass. The shaft of a rotating unit spins at angular velocity  $\omega_1$ , whereas, a floating ring bearing spins at angular speed  $\omega_2$ . The angular velocity  $\omega_2$  has been determined from the equilibrium of friction moments on both the outer and inner surfaces of a floating ring bearing. A mathematical model constitutes a system of differential equations, mutually coupled. The mathematical model has been solved by determining acceleration, velocity and displacement in each node. This work deals with the influence of the imbalance of rotating elements, bearings clearances, rotational speed of a shaft on rigidity and

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damping factors of bearing supports as well as the amplitude of displacements in nodes of rotating units. Having analysed the results of the research, we noticed the crucial influence of imbalance and a quotient of radial clearances on displacement amplitude in bearing nodes. Also, it has been stated that the growth of quotient of radial clearances causes the growth of displacement amplitude.

## 1. Introduction

From the point of the generation of oscillation, a turbocharger is a self-generating system. The essential source of oscillations is rotating units [3], [5], [7], [10] with bearings. Because of the simple structure, good dynamic properties [1], [2], [6], [11], and good heat transmission in these types of structures, we use sliding bearings with a floating ring bearing. Good examples are turbochargers installed in engines of cars and fishing boats (Fig.1).

This research deals with the influence of the imbalance of rotating elements, bearing clearances, the rotational speed of a shaft, bearings load on rigidity and damping factors in bearing supports and also displacements amplitude in nodes of the rotating units.

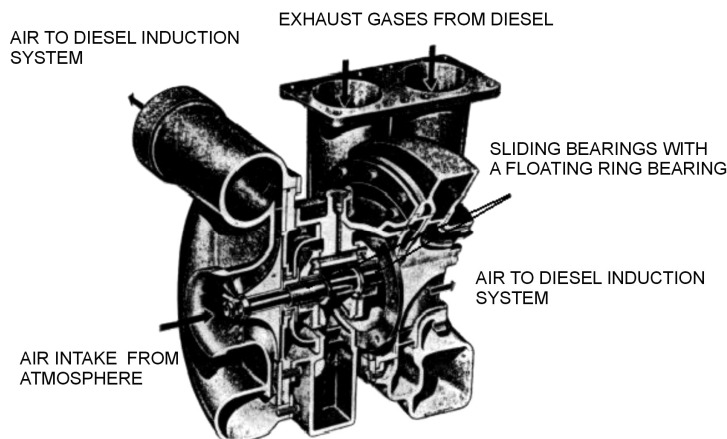


Fig. 1. Section of a C0 -45 turbocharger  
Rys. 1. Przekrój turbosprężarki C0-45

## 2. Dynamic model of rotating unit in a turbocharger

The discussed model of the rotating unit has been described in the Fig.2. In this model, each bearing is modelled including a floating ring bearing mass. Through rigidity and damping factors, oil films capacity towards oscillations damping has been also considered. The motion of the model has been examined in two planes: 0XZ and 0YZ.

Each of rotors with masses distributed in a constant way has been replaced with a concentrated mass found in the center of mass. Thus, a compressor rotor has been replaced with mass  $m_4$  and a turbine rotor with  $m_1$ . A distributed mass of a shaft has been replaced with two masses  $m_2, m_3$ . Floating ring bearings have masses  $m_5$  and  $m_6$ . Shaft sections among supports have been treated as components with constant stiffness  $E \cdot I$ . Driving forces, which affect masses  $m_1$  and  $m_4$ , constitute either forces of gravity or forces deriving from the imbalance of rotating masses. Having assumed that additional masses  $m_{n1}$  and  $m_{n4}$  are placed respectively at distances  $\delta_1$  and  $\delta_4$ , the effect of dynamic imbalance [10] has been ignored. The action of each point mass constitutes an outer driving force that equals  $m_{n1} \cdot \delta_1 \cdot \omega_1^2$  and  $m_{n4} \cdot \delta_4 \cdot \omega_1^2$ . Having assumed that these forces do not act together in a phase, and the angle of displacement phase is represented by  $\varphi$ .

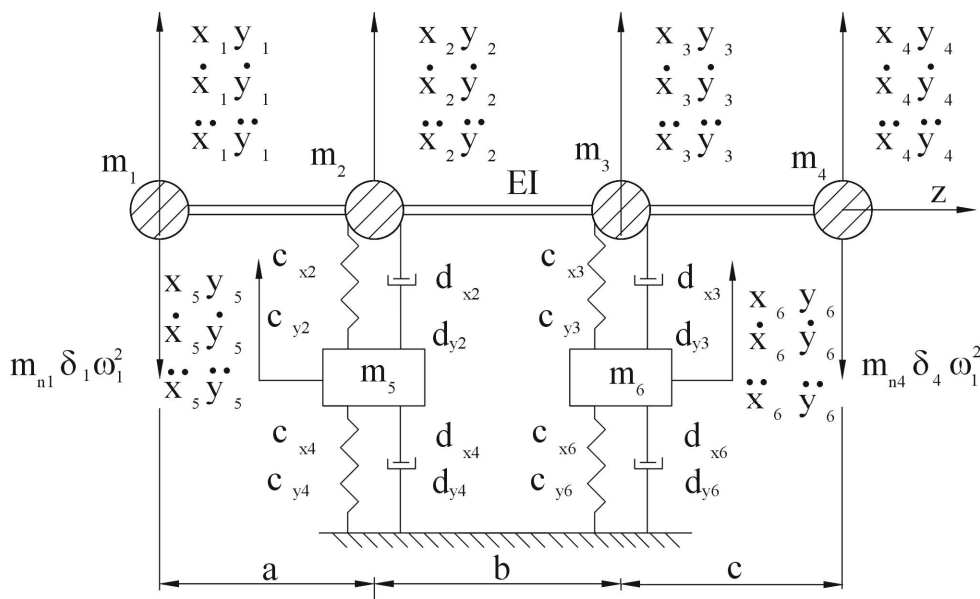


Fig. 2. The model of a rotating unit  
Rys. 2. Model zespołu wirującego

### 3. Mathematical model of a turbocharger rotating unit

Motion equations for the discrete model have been described in Fig. 2 and have been written by the force method for each mass model. In planes  $OXZ$  and  $OYZ$ , these equations are written in the form:

$$\begin{aligned}
x_1 &= -\alpha_{x11} [m_1 \ddot{x}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t] - \alpha_{x12} [m_2 \ddot{x}_2 + d_{x2} (\dot{x}_2 - \dot{x}_5)] - \alpha_{x13} [m_3 \ddot{x}_3 + d_{x3} (\dot{x}_3 - \dot{x}_6)] - \\
&- \alpha_{x14} [m_4 \ddot{x}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t] \\
x_2 &= -\alpha_{x21} [m_1 \ddot{x}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t] - \alpha_{x22} [m_2 \ddot{x}_2 + d_{x2} (\dot{x}_2 - \dot{x}_5)] - \alpha_{x23} [m_3 \ddot{x}_3 + d_{x3} (\dot{x}_3 - \dot{x}_6)] - \\
&- \alpha_{x24} [m_4 \ddot{x}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t] \\
x_3 &= -\alpha_{x31} [m_1 \ddot{x}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t] - \alpha_{x32} [m_2 \ddot{x}_2 + d_{x2} (\dot{x}_2 - \dot{x}_5)] - \alpha_{x33} [m_3 \ddot{x}_3 + d_{x3} (\dot{x}_3 - \dot{x}_6)] - \\
&- \alpha_{x34} [m_4 \ddot{x}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t] \\
x_4 &= -\alpha_{x41} [m_1 \ddot{x}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t] - \alpha_{x42} [m_2 \ddot{x}_2 + d_{x2} (\dot{x}_2 - \dot{x}_5)] - \alpha_{x43} [m_3 \ddot{x}_3 + d_{x3} (\dot{x}_3 - \dot{x}_6)] - \\
&- \alpha_{x44} [m_4 \ddot{x}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t] \\
m_5 \ddot{x}_5 + c_{x4} \dot{x}_5 + d_{x4} \dot{x}_5 + c_{x2} (x_5 - x_2) + d_{x2} (\dot{x}_5 - \dot{x}_2) &= 0 \\
m_6 \ddot{x}_6 + c_{x6} \dot{x}_6 + d_{x6} \dot{x}_6 + c_{x3} (x_6 - x_3) + d_{x3} (\dot{x}_6 - \dot{x}_3) &= 0 \\
y_1 &= -\alpha_{x11} [m_1 \ddot{y}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t + Q_1] - \alpha_{x12} [m_2 \ddot{y}_2 + d_{x2} (\dot{y}_2 - \dot{y}_5) + Q_2] - \\
&- \alpha_{x13} [m_3 \ddot{y}_3 + d_{x3} (\dot{y}_3 - \dot{y}_6) + Q_3] - \alpha_{x14} [m_4 \ddot{y}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t + Q_4] \\
y_2 &= -\alpha_{x21} [m_1 \ddot{y}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t + Q_1] - \alpha_{x22} [m_2 \ddot{y}_2 + d_{x2} (\dot{y}_2 - \dot{y}_5) + Q_2] - \\
&- \alpha_{x23} [m_3 \ddot{y}_3 + d_{x3} (\dot{y}_3 - \dot{y}_6) + Q_3] - \alpha_{x24} [m_4 \ddot{y}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t + Q_4] \\
y_3 &= -\alpha_{x31} [m_1 \ddot{y}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t + Q_1] - \alpha_{x32} [m_2 \ddot{y}_2 + d_{x2} (\dot{y}_2 - \dot{y}_5) + Q_2] - \\
&- \alpha_{x33} [m_3 \ddot{y}_3 + d_{x3} (\dot{y}_3 - \dot{y}_6) + Q_3] - \alpha_{x34} [m_4 \ddot{y}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t + Q_4] \\
y_4 &= -\alpha_{x41} [m_1 \ddot{y}_1 - m_{n1} \delta_1 \omega^2 \sin \omega t + Q_1] - \alpha_{x42} [m_2 \ddot{y}_2 + d_{x2} (\dot{y}_2 - \dot{y}_5) + Q_2] - \\
&- \alpha_{x43} [m_3 \ddot{y}_3 + d_{x3} (\dot{y}_3 - \dot{y}_6) + Q_3] - \alpha_{x44} [m_4 \ddot{y}_4 - m_{n4} \delta_4 \omega^2 \sin \omega t + Q_4] \\
m_5 \ddot{y}_5 + c_{y4} \dot{y}_5 + d_{y4} \dot{y}_5 + c_{y2} (y_5 - y_2) + d_{y2} (\dot{y}_5 - \dot{y}_2) &= Q_5 \\
m_6 \ddot{y}_6 + c_{y6} \dot{y}_6 + d_{y6} \dot{y}_6 + c_{y3} (y_6 - y_3) + d_{y3} (\dot{y}_6 - \dot{y}_3) &= Q_6
\end{aligned} \tag{1}$$

Whereas, motion equations for the discrete model written as a matrix in planes 0XZ and 0YZ have the form:

$$\begin{aligned}
[M_x] \cdot [\ddot{x}] + [D_{xx}] \cdot [\dot{x}] + [D_{xy}] \cdot [\dot{x}] + [C_{xx}] \cdot [x] + [C_{xy}] \cdot [x] &= [F_x(t)], \\
[M_y] \cdot [\ddot{y}] + [D_{yy}] \cdot [\dot{y}] + [D_{yx}] \cdot [\dot{y}] + [C_{yy}] \cdot [y] + [C_{yx}] \cdot [y] &= [F_y(t)],
\end{aligned} \tag{2}$$

The description of particular elements of a matrix of the equation 2 is presented in the work [9]. In the mathematical model of a bearing unit, we have considered impact factors  $\alpha_{xrs}$ ,  $\alpha_{yrs}$  (where; x -defines plane 0XZ, y-defines plane 0YZ, r = 1, 2, 3, 4, s = 1, 2, 3, 4) that are deflections measured in a specific s-point, which result from the application of elementary force F=1 [N] in a specific r-point Fig. 2.

Impact factors for plane 0XZ are:

$$\begin{aligned}
 \alpha_{x11} &= \frac{a^2(a+b)}{3EI} + \frac{(a+b)^2}{c_{x2}b^2} + \frac{a^2}{c_{x3}b^2}, & \alpha_{x12} &= \alpha_{x21} = \frac{a+b}{c_{x2}b} \\
 \alpha_{x13} &= \alpha_{x31} = \frac{-a}{c_{x2}b}, & \alpha_{x14} &= \alpha_{x41} = \frac{abc}{6EI} - \frac{(a+b)c}{c_{x2}b^2} - \frac{(b+c)a}{c_{x3}b^2}, \\
 \alpha_{x22} &= \frac{1}{c_{x2}}, & \alpha_{x23} &= \alpha_{x32} = 0, & \alpha_{x42} &= \alpha_{x24} = \frac{-c}{c_{x2}b}, & \alpha_{x33} &= \frac{1}{c_{x3}}, \\
 \alpha_{x43} &= \alpha_{x34} = \frac{b+c}{c_{x3}b}, & \alpha_{x44} &= \frac{a^2(b+c)}{3EI} + \frac{(b+c)^2}{c_{x3}b^2} + \frac{c^2}{c_{x2}b^2},
 \end{aligned} \tag{3}$$

For plane 0YZ impact factors  $\alpha_{yrs} = \alpha_{ysr}$  by using the substitution  $k_{x2} = k_{y2}$ , and  $k_{x3} = k_{y3}$  we obtain the equation (2).

Substitute rigidity factors ( $c_{x2}$ ,  $c_{x3}$ ,  $c_{x4}$ ,  $c_{x6}$ ,  $c_{y2}$ ,  $c_{y3}$ ,  $c_{y4}$ ,  $c_{y6}$ ) and substitute damping factors of oil film ( $d_{x2}$ ,  $d_{x3}$ ,  $d_{x4}$ ,  $d_{x6}$ ,  $d_{y2}$ ,  $d_{y3}$ ,  $d_{y4}$ ,  $d_{y6}$ ) for planes 0XZ and 0YZ are equal:

$$\begin{aligned}
 c_{x2} &= \frac{c_{xx}(1,1) \cdot (x_2 - x_5) + c_{xy}(1,1) \cdot (y_2 - y_5)}{(x_2 - x_5)}, \\
 c_{x3} &= \frac{c_{xx}(2,1) \cdot (x_3 - x_6) + c_{xy}(2,1) \cdot (y_3 - y_6)}{(x_3 - x_6)}, \\
 c_{x4} &= \frac{c_{xx}(1,2) \cdot x_5 + c_{xy}(1,2) \cdot y_5}{x_5}, \\
 c_{x6} &= \frac{c_{xx}(2,2) \cdot x_6 + c_{xy}(2,2) \cdot y_6}{x_6}, \\
 c_{y2} &= \frac{c_{yx}(1,1) \cdot (x_2 - x_5) + c_{yy}(1,1) \cdot (y_2 - y_5)}{(y_2 - y_5)}, \\
 c_{y3} &= \frac{c_{yx}(2,1) \cdot (x_3 - x_6) + c_{yy}(2,1) \cdot (y_3 - y_6)}{(y_3 - y_6)}, \\
 c_{y4} &= \frac{c_{yx}(1,2) \cdot x_5 + c_{yy}(1,2) \cdot y_5}{y_5}, & c_{y6} &= \frac{c_{yx}(2,2) \cdot x_6 + c_{yy}(2,2) \cdot y_6}{y_6}, \\
 d_{x3} &= \frac{d_{xx}(2,1) \cdot (\dot{x}_3 - \dot{x}_6) + d_{xy}(2,1) \cdot (\dot{y}_3 - \dot{y}_6)}{(\dot{x}_3 - \dot{x}_6)},
 \end{aligned} \tag{4}$$

$$d_{x2} = \frac{d_{xx}(1,1) \cdot (\dot{x}_2 - \dot{x}_5) + d_{xy}(1,1) \cdot (\dot{y}_2 - \dot{y}_5)}{(\dot{x}_2 - \dot{x}_5)},$$

$$d_{x4} = \frac{d_{xx}(1,2) \cdot \dot{x}_5 + d_{xy}(1,2) \cdot \dot{y}_5}{\dot{x}_5},$$

$$d_{x6} = \frac{d_{xx}(2,2) \cdot \dot{x}_6 + d_{xy}(2,2) \cdot \dot{y}_6}{\dot{x}_6}, \quad d_{y3} = \frac{d_{yx}(2,1) \cdot (\dot{x}_3 - \dot{x}_6) + d_{yy}(2,1) \cdot (\dot{y}_3 - \dot{y}_6)}{(\dot{y}_3 - \dot{y}_6)},$$

$$d_{y2} = \frac{d_{yx}(1,1) \cdot (\dot{x}_2 - \dot{x}_5) + d_{yy}(1,1) \cdot (\dot{y}_2 - \dot{y}_5)}{(\dot{y}_2 - \dot{y}_5)},$$

$$d_{y4} = \frac{d_{yx}(1,2) \cdot \dot{x}_5 + d_{yy}(1,2) \cdot \dot{y}_5}{\dot{y}_5},$$

$$d_{y6} = \frac{d_{yx}(2,2) \cdot \dot{x}_6 + d_{yy}(2,2) \cdot \dot{y}_6}{\dot{y}_6},$$

where:  $c_{xx}, c_{xy}$  are rigidity factors of oil film in plane OXZ,  
 $c_{yx}, c_{yy}$  are rigidity factors of oil film in plane OYZ,  
 $d_{xx}, d_{xy}$  are damping factors of oil film in plane OXZ,  
 $d_{yx}, d_{yy}$  are damping factors of oil film in plane OYZ,

Factors  $c_{xy}, d_{xy}$  consider the impact of acting forces in plane OYZ on displacements in plane OXZ. While, factors  $c_{yx}, d_{yx}$  determine the influence of acting forces in plane OXZ on displacements in plane OYZ.

#### 4. Rigidity and damping factors of the sliding bearing with a floating ring bearing

Constructional elements of a bearing are (Fig.3) journal (1), fixed bearing bush (3), and loosely fixed floating ring (2) separating journal and the fixed bearing bush, known as floating ring bearing. The oil is supplied into outer and inner bearing under the pressure through holes (4), which are in fixed bearing bush and floating ring bearing. Circumferential grooves (5) in the fixed bearing bush or floating ring bearing provide regular oil feed to lubricant gaps. Directions of oil flow in a bearing (6).

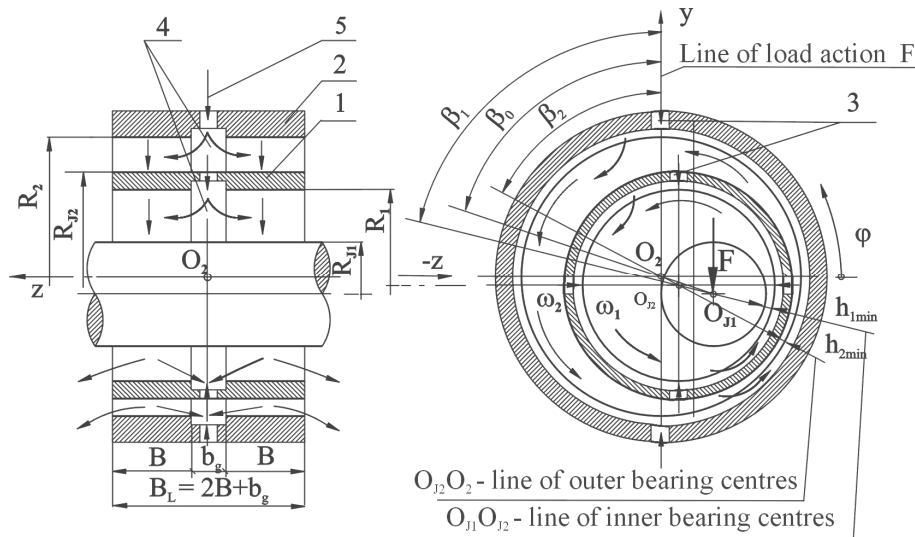


Fig. 3. The sliding bearing with a floating ring bearing  
 Rys. 3. Łożysko ślizgowe z panewką pływającą

Resultant pressure in oil films and hydrodynamic bearing load capacity ( $F_L$ ) balances a bearing outer load ( $F$ ), which is attached to a bearing journal. The isothermal model of a short bearing [4] has been accepted to calculate the work parameters in a static equilibrium. Forces and the moment system are described in Fig. 4.

Work parameters of a bearing are described by forces and moment equations:

$$\text{Sommerfeld Number for inner oil film } S_{o1} = \frac{\eta(\omega_1 + \omega_2) \cdot D_1 B}{F} \left( \frac{R_1}{C_{R1}} \right)^2 \quad (5)$$

$$\text{Sommerfeld Number for outer oil film } S_{o2} = \frac{\eta\omega_2 D_2 B}{F} \left( \frac{R_3}{C_{R2}} \right)^2 \quad (6)$$

Equations of balance of forces are:

$$\pi \left( \frac{B}{D_2} \right) \cdot S_{o1} = \frac{(1 - \varepsilon_1^2)^2}{\varepsilon_1 \sqrt{16\varepsilon_1^2 + \pi^2 (1 - \varepsilon_1^2)}} \quad (7)$$

$$\pi \left( \frac{B}{D_2} \right) \cdot S_{02} = \frac{(1 - \varepsilon_2^2)^2}{\varepsilon_1 \sqrt{16\varepsilon_2^2 + \pi^2(1 - \varepsilon_2^2)}} \quad (8)$$

Equations of the equilibrium of moments on the outer and inner surfaces of a floating ring bearing  $M_2(O_{J2}) = M_3(O_{J2})$  are:

$$S_{02} \cdot \pi \int_0^{2\pi} \frac{l}{B(1 + \varepsilon_2 \cos \varphi_2)} \frac{d\varphi_2}{2} + \frac{1}{2} \varepsilon_2 \cos \beta_2 = \left( \frac{C_{R1}}{C_{R2}} \right) \left( \frac{1 - \nu}{1 - \nu} S_{01} \pi \int_0^{2\pi} \frac{l}{B(1 + \varepsilon_1 \cos \varphi_1)} \frac{d\varphi_1}{2} - \frac{1}{2} \varepsilon_1 \cos \beta_1 \right) \quad (9)$$

where

$$\nu = \frac{\omega_2}{\omega_1}, \quad \text{ctg} \beta_1 = \frac{\pi \cdot \sqrt{1 - \varepsilon_1^2}}{4 \cdot \varepsilon_1}, \quad \text{ctg} \beta_2 = \frac{\pi \cdot \sqrt{1 - \varepsilon_2^2}}{4 \cdot \varepsilon_2}, \quad (10)$$

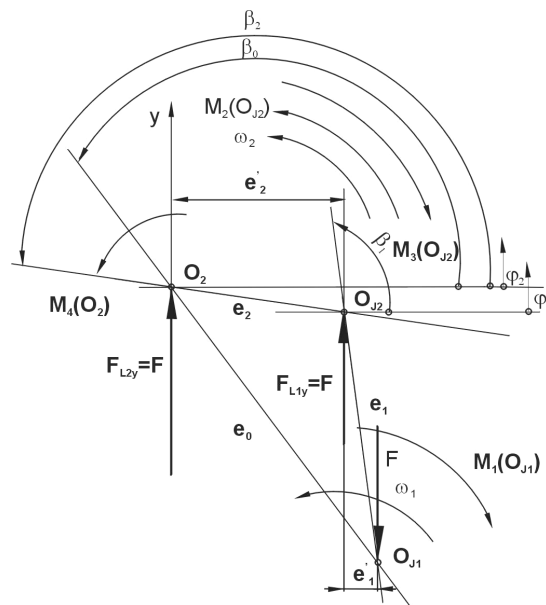


Fig. 4. Forces and moments system in a bearing  
Rys. 4. Układ sił i momentów w łożysku

## 5. Research of dynamic properties

The analysis of dynamic properties of a rotating unit in Fig.1 has been carried out for structural cases described in Chart 1.



Chart 1. Given parameters from calculations of the rotating unit  
Tabela 1. Parametry zadane od obliczeń zespołu wirującego

<b>Concentrated masses in particular nodes [N·s<sup>2</sup>/m]</b>					
$m_1$	$m_2$	$m_3$	$m_4$	$m_5$	$m_6$
5.0	0.3	0.25	2.0	0.055	0.055
<b>Bearing loads [N]</b>					
in the second node $F = 400, 600$			In the third node $F = 370, 550$		
<b>Radial clearances in bearings [m]</b>					
$C_{R1} = 0.1 \cdot 10^{-3}, 0.17 \cdot 10^{-3}$			$C_{R2} = 0.06 \cdot 10^{-3}, 0.3 \cdot 10^{-3}$		
<b>Journal radiuses for inner bearing and outer bearing [m]</b>					
$R_{J1} = 15.82 \cdot 10^{-3}$ [m]			$R_{J1} = 18.89 \cdot 10^{-3}$ [m]		
<b>Bearings width [m]</b>					
in the second node $B = 0.174$			in the third node $B = 0.174$		
<b>Geometric parameters of rotating unit</b>					
$a = 0.055$ [m]	$b = 0.075$ [m]	$c = 0.045$ [m]	$I_x = 0.15 \cdot 10^{-6}$ [m <sup>4</sup> ]		
<b>Material constants</b>					
$E = 1.915 \cdot 10^{11}$ [N/m <sup>2</sup> ]			$\eta = 0.028$ [Pa·s]		
<b>Rotational speed of a shaft [rpm]</b>					
$N_i = 500, 400$					
<b>Imbalance of rotating masses [N·s<sup>2</sup>]</b>					
$N_{w1} = 0.18 \cdot 10^{-4}, 0.88 \cdot 10^{-4}$			$N_{w4} = 0.5 \cdot 10^{-5}, 0.65 \cdot 10^{-4}$		

For the presented given parameters in Chart 1, the following have been determined: rigidity and damping factors in bearings supports and amplitudes and displacement phases as well as acceleration and velocity phases in particular nodes. Moreover, the stability of the rotating unit has been checked. The results are given in Charts 2- 4.

Chart 2. Stiffness and damping factors  
Tabela 2. Współczynniki sztywności i tłumienia

<b>Given parameters</b>						
	<b>Task 1</b>	<b>Task 2</b>	<b>Task 3</b>	<b>Task 4</b>	<b>Task 5</b>	<b>Task 6</b>
[N·s <sup>2</sup> ]	$N_{w1} = 0.18 \cdot 10^{-4}$	$N_{w1} = 0.18 \cdot 10^{-4}$	$N_{w1} = 0.18 \cdot 10^{-4}$	$N_{w1} = 0.18 \cdot 10^{-4}$	$N_{w1} = 0.18 \cdot 10^{-4}$	$N_{w1} = 0.88 \cdot 10^{-4}$
[N·s <sup>2</sup> ]	$N_{w2} = 0.5 \cdot 10^{-5}$	$N_{w2} = 0.5 \cdot 10^{-5}$	$N_{w2} = 0.5 \cdot 10^{-5}$	$N_{w2} = 0.5 \cdot 10^{-5}$	$N_{w2} = 0.5 \cdot 10^{-5}$	$N_{w2} = 0.5 \cdot 10^{-5}$
[rpm]	$N_i = 500$	$N_i = 500$	$N_i = 400$	$N_i = 500$	$N_i = 500$	$N_i = 400$
[N]	in the second node $F = 400$	in the second node $F = 600$	in the second node $F = 400$	In the second node $F = 400$	in the second node $F = 400$	in the second node $F = 400$
[N]	in the third node $F = 370$	in the third node $F = 550$	in the third node $F = 370$	In the third node $F = 370$	in the third node $F = 370$	in the third node $F = 370$
[m]	$C_{R1} = 0.1 \cdot 10^{-3}$	$C_{R1} = 0.1 \cdot 10^{-3}$	$C_{R1} = 0.1 \cdot 10^{-3}$	$C_{R1} = 0.17 \cdot 10^{-3}$	$C_{R1} = 0.1 \cdot 10^{-3}$	$C_{R1} = 0.1 \cdot 10^{-3}$
[m]	$C_{R2} = 0.06 \cdot 10^{-3}$	$C_{R2} = 0.06 \cdot 10^{-3}$	$C_{R2} = 0.06 \cdot 10^{-3}$	$C_{R2} = 0.06 \cdot 10^{-3}$	$C_{R2} = 0.3 \cdot 10^{-3}$	$C_{R2} = 0.06 \cdot 10^{-3}$

Given parameters						
	Task 1	Task 2	Task 3	Task 4	Task 5	Task 6
<b>Stiffness and damping factors: J=1, I=1</b>						
$b_{xx}$ [N·s/m]	4520	10320	8765	4297	6468	8765
$b_{xy}$ [N·s/m]	2415	3514	2970	1368	2071	2970
$b_{yx}$ [N·s/m]	2415	3514	2970	1368	2071	2970
$b_{yy}$ [N·s/m]	7301	5118	4819	1393	4340	4819
$k_{xx}$ [N/m]	$8.718 \cdot 10^6$	$1.6335 \cdot 10^7$	$9.838 \cdot 10^6$	$9.633 \cdot 10^6$	$8.014 \cdot 10^6$	$9.838 \cdot 10^6$
$k_{xy}$ [N/m]	$1.632 \cdot 10^7$	$2.382 \cdot 10^7$	$1.597 \cdot 10^7$	$9.807 \cdot 10^6$	$1.68 \cdot 10^7$	$1.597 \cdot 10^7$
$k_{yx}$ [N/m]	$-6.735 \cdot 10^6$	$-6.113 \cdot 10^6$	$-5.162 \cdot 10^6$	$-5.957 \cdot 10^5$	$-8.113 \cdot 10^6$	$-5.162 \cdot 10^6$
$k_{yy}$ [N/m]	$9.328 \cdot 10^6$	$1.343 \cdot 10^7$	$9.126 \cdot 10^6$	$4.891 \cdot 10^6$	$9.469 \cdot 10^6$	$9.126 \cdot 10^6$
<b>Stiffness and damping factors: J=1, I=2</b>						
$b_{xx}$ [N·s/m]	58560	89540	73510	85210	8061	7351
$b_{xy}$ [N·s/m]	19930	29550	24740	28280	1703	24740
$b_{yx}$ [N·s/m]	19930	29550	24740	28280	1703	24740
$b_{yy}$ [N·s/m]	28660	33910	31300	33230	875.1	31300
$k_{xx}$ [N/m]	$1.84 \cdot 10^7$	$3.535 \cdot 10^7$	$2.107 \cdot 10^7$	$2.292 \cdot 10^7$	$1.508 \cdot 10^7$	$2.107 \cdot 10^7$
$k_{xy}$ [N/m]	$2.647 \cdot 10^7$	$4.057 \cdot 10^7$	$2.666 \cdot 10^7$	$2.693 \cdot 10^7$	$7.753 \cdot 10^6$	$2.666 \cdot 10^7$
$k_{yx}$ [N/m]	$-6.588 \cdot 10^6$	$-4.887 \cdot 10^6$	$-4.636 \cdot 10^6$	$-3.582 \cdot 10^6$	$-1.193 \cdot 10^6$	$-4.636 \cdot 10^6$
$k_{yy}$ [N/m]	$1.489 \cdot 10^6$	$2.134 \cdot 10^7$	$1.452 \cdot 10^7$	$1.43 \cdot 10^7$	$2.405 \cdot 10^6$	$1.452 \cdot 10^7$
<b>Stiffness and damping factors: J=2, I=1</b>						
$b_{xx}$ [N·s/m]	6885	9533	73510	3952	6126	8204
$b_{xy}$ [N·s/m]	2247	3243	24740	1273	1920	2763
$b_{yx}$ [N·s/m]	2247	3243	24740	1273	1920	2763
$b_{yy}$ [N·s/m]	4431	4969	31300	1343	4264	4707
$k_{xx}$ [N/m]	$7.745 \cdot 10^6$	$1.427 \cdot 10^7$	$8.717 \cdot 10^6$	$2.292 \cdot 10^7$	$7.13 \cdot 10^6$	$8.817 \cdot 10^6$
$k_{xy}$ [N/m]	$1.528 \cdot 10^7$	$2.186 \cdot 10^7$	$1.485 \cdot 10^7$	$2.693 \cdot 10^7$	$1.583 \cdot 10^7$	$1.485 \cdot 10^7$
$k_{yx}$ [N/m]	$-6.808 \cdot 10^6$	$-6.289 \cdot 10^6$	$-5.252 \cdot 10^6$	$-3.582 \cdot 10^6$	$-8.2 \cdot 10^6$	$-5.252 \cdot 10^6$
$k_{yy}$ [N/m]	$8.691 \cdot 10^6$	$1.243 \cdot 10^7$	$8.508 \cdot 10^6$	$1.43 \cdot 10^7$	$8.818 \cdot 10^6$	$8.508 \cdot 10^6$
<b>Stiffness and damping factors: J=2, I=2</b>						
$b_{xx}$ [N·s/m]	54320	81400	67760	78390	7241	67760
$b_{xy}$ [N·s/m]	18490	27140	22940	26240	1563	22940
$b_{yx}$ [N·s/m]	18490	27140	22940	26240	1563	22940
$b_{yy}$ [N·s/m]	27870	32610	30320	32120	826.6	30320
$k_{xx}$ [N/m]	$1.625 \cdot 10^7$	$3.072 \cdot 10^7$	$1.859 \cdot 10^7$	$2.023 \cdot 10^7$	$1.331 \cdot 10^7$	$1.859 \cdot 10^7$
$k_{xy}$ [N/m]	$2.45 \cdot 10^7$	$3.691 \cdot 10^7$	$2.457 \cdot 10^7$	$2.476 \cdot 10^7$	$7.037 \cdot 10^6$	$2.457 \cdot 10^7$
$k_{yx}$ [N/m]	$-6.801 \cdot 10^6$	$-5.354 \cdot 10^6$	$-4.885 \cdot 10^6$	$-3.848 \cdot 10^6$	$-1.047 \cdot 10^6$	$-4.885 \cdot 10^6$
$k_{yy}$ [N/m]	$1.389 \cdot 10^7$	$1.975 \cdot 10^7$	$1.355 \cdot 10^7$	$1.334 \cdot 10^7$	$2.235 \cdot 10^6$	$1.355 \cdot 10^7$
<b>Stability research of rotating unit</b>						
	unstable	stable	stable	stable	stable	stable

Chart 3. The influence of rotors imbalance on displacement amplitude in nodes of rotating unit  
Tabela 3. Wpływ niewyważenia wirników na amplitudę przemieszczeń w węzłach zespołu wirującego

	Displacement amplitude in nodes of rotating unit [m]					
	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$
	$y_1$	$y_2$	$y_3$	$y_4$	$y_5$	$y_6$
<b>Task 3</b>	$2.267 \cdot 10^{-6}$	$1.266 \cdot 10^{-6}$	$1.162 \cdot 10^{-6}$	$2.344 \cdot 10^{-6}$	<b><math>0.2682 \cdot 10^{-6}</math></b>	<b><math>0.2351 \cdot 10^{-6}</math></b>
<b>Task 6</b>	$6.908 \cdot 10^{-6}$	$6.19 \cdot 10^{-6}$	$8.431 \cdot 10^{-6}$	$13.16 \cdot 10^{-6}$	<b><math>1.577 \cdot 10^{-6}</math></b>	<b><math>2.076 \cdot 10^{-6}</math></b>
<b>Task 3</b>	$3.641 \cdot 10^{-6}$	$3.185 \cdot 10^{-6}$	$2.971 \cdot 10^{-6}$	$3.203 \cdot 10^{-6}$	<b><math>0.5455 \cdot 10^{-6}</math></b>	<b><math>0.3799 \cdot 10^{-6}</math></b>
<b>Task 6</b>	$17.63 \cdot 10^{-6}$	$22.04 \cdot 10^{-6}$	$29.43 \cdot 10^{-6}$	$34.82 \cdot 10^{-6}$	<b><math>3.441 \cdot 10^{-6}</math></b>	<b><math>4.067 \cdot 10^{-6}</math></b>

Chart 4. The influence of radial clearances on displacement amplitude in nodes of rotating unit  
Tabela 4. Wpływ luzów promieniowych na amplitudę przemieszczeń w węzłach zespołu wirującego

	Displacement amplitude in nodes of rotating unit [m]					
	x <sub>1</sub>	x <sub>2</sub>	x <sub>3</sub>	x <sub>4</sub>	x <sub>5</sub>	x <sub>6</sub>
	y <sub>1</sub>	y <sub>2</sub>	y <sub>3</sub>	y <sub>4</sub>	y <sub>5</sub>	y <sub>6</sub>
<b>Task 2</b>	2.33·10 <sup>-6</sup>	1.437·10 <sup>-6</sup>	1.445·10 <sup>-6</sup>	2.785·10 <sup>-6</sup>	<b>0.2872·10<sup>-6</sup></b>	<b>0.2733·10<sup>-6</sup></b>
<b>Task 4</b>	3.277·10 <sup>-6</sup>	2.838·10 <sup>-6</sup>	2.645·10 <sup>-6</sup>	3.03·10 <sup>-6</sup>	<b>0.2636·10<sup>-6</sup></b>	<b>0.2508·10<sup>-6</sup></b>
<b>Task 5</b>	3.557·10 <sup>-6</sup>	3.196·10 <sup>-6</sup>	2.86·10 <sup>-6</sup>	2.85·10 <sup>-6</sup>	<b>1.43610<sup>-6</sup></b>	<b>1.228·10<sup>-6</sup></b>
<b>Task 2</b>	3.745·10 <sup>-6</sup>	3.3·10 <sup>-6</sup>	3.096·10 <sup>-6</sup>	3.35·10 <sup>-6</sup>	<b>0.5687·10<sup>-6</sup></b>	<b>0.3973·10<sup>-6</sup></b>
<b>Task 4</b>	3.816·10 <sup>-6</sup>	3.509·10 <sup>-6</sup>	3.219·10 <sup>-6</sup>	3.14·10 <sup>-6</sup>	<b>0.2088·10<sup>-6</sup></b>	<b>0.1646·10<sup>-6</sup></b>
<b>Task 5</b>	3.606·10 <sup>-6</sup>	3.264·10 <sup>-6</sup>	2.806·10 <sup>-6</sup>	2.54·10 <sup>-6</sup>	<b>3.88·10<sup>-6</sup></b>	<b>3.265·10<sup>-6</sup></b>

## Conclusions

The case study of a rotating unit running at high rotating speed ( $n=400 - 500$  rpm) and under light load  $F = <370 - 600>$  [N] has been considered. The analysis of the research results indicates the following:

- Structural sample No1 is the unstable example. The stability of a rotating units (structural tasks 2, 3, 4, 5, 6) has been achieved due to the boost in bearings load, the reduction in rotational speed of a shaft, and the boost of radial clearances.
- The value of rotors' imbalance (Tasks 1 -6) has an essential influence on oscillation level. The amplitude of displacements (Chart 3) in the node 4 for a coordinate  $y_4$  has increased by 11 times.
- The rapid growth in the value of the quotient of radial clearances causes the growth of displacements amplitude in nodes (5 and 6) which form bearings supports.

The concluding remarks are as follows:

- A journal bearing geometry has a significant impact on the amplitude of displacements in the bearing nodes and, in consequence, on the proper operation of a turbocharger,
- The imbalance of rotating masses has an unfavourable influence on the vibration level of the rotating unit of a turbocharger.

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### **Badanie właściwości dynamicznych zespołów wirujących turbosprężarek**

#### **Streszczenie**

Opracowano model dynamiczny zespołu wirującego turbosprężarki. Masę wirników i wału zamodelowano jako masy skupione. Zespół wirujący został podparty na dwóch podporach stanowiących poprzeczne łożyska ślizgowe z panewką pływającą. Każde łożysko zamodelowano uwzględniając masę panewki pływającej. Wał zespołu wirującego obraca się z prędkością kątową  $\omega_1$ , natomiast panewka pływająca z prędkością kątową  $\omega_2$ . Prędkość kątowa  $\omega_2$  wyznaczona została z równowagi momentów tarcia na powierzchni zewnętrznej i wewnętrznej panewki pływającej. Model matematyczny stanowi układ równań różniczkowych, wzajemnie sprzężonych. Model matematyczny rozwiązano wyznaczając w każdym węźle: przyspieszenie, prędkości i przemieszczenia. W pracy przedstawiono wpływ: niewyważenia elementów wirujących, luzów łożyskowych, prędkości obrotowej wału na współczynniki sztywności i tłumienia podpór łożyskowych oraz amplitudę przemieszczeń węzłów zespołu wirującego. Analizując wyniki badań stwierdzono wpływ niewyważenia i ilorazu luzów promieniowych na amplitudę przemieszczeń w węzłach łożyskowych. Ze wzrostem ilorazu luzów promieniowych i niewyważenia rosną amplitudy przemieszczeń.